### Solution

By using formula of power

Power = 
$$\frac{Work}{time}$$
  

$$P = \frac{W}{t}$$

$$P = \frac{FS}{t}$$

$$P = \frac{mgh}{t} \quad \because F = W = mg \& S = h$$

Power = P = ?

5.4. A body of mass 20 kg is at rest. A 40 N force acts on it for 5 seconds. What is the kinetic energy of the body at the end of this time?

Mass of body = 
$$m = 20 \text{ kg}$$
  
Initial velocity =  $v_i = 0 \text{ ms}^{-1}$   
Force =  $F = 40 \text{ N}$   
Time =  $t = 5 \text{ s}$ 

To Find

**Given Data** 

Kinetic energy = 
$$E_k = ?$$

# Solution

By using second law of motion

$$F = ma$$

$$40 = (20)(a)$$

$$\frac{40}{20} = a$$

$$2 = a$$

$$a = 2 ms^{-2}$$

For final velocity using first equation of motion

$$v_f = v_i + gt$$
  
 $v_f = 0 + (2)(5)$   
 $v_f = 10 ms^{-1}$   
 $v = 10 ms^{-1}$ 

Now, by using formula of kinetic energy

$$E_k = \frac{1}{2}mv^2$$

$$E_k = \frac{1}{2}(20)(10)^2$$

$$E_k = \frac{1}{2}(20)(100)$$

$$E_k = \mathbf{1000}J$$

5.5. A ball of mass 160 g is thrown vertically upward. The ball reaches a height of 20 m. Find the potential energy gained by the ball at this height.

## Given Data

Mass of ball = 
$$m = 160 g$$
  

$$m = \frac{160}{1000} kg$$

$$m = 0.16 kg$$

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 $Height\ reached = h = 20\ m$ 

Gravitational acceleration =  $g = 10 \text{ ms}^{-2}$ 

To Find

Potential energy = 
$$E_p$$
 = ?

**Important Formulas** 

$$ightharpoonup Work Done W = FS \implies W = FS \cos \theta$$

$$Figure 1.5 Figure 2.5 Fig$$

$$ightharpoonup$$
 Potential Energy  $E_p=mgh$ 

$$ightharpoonup$$
 Mass Energy Equation  $E=mc^2$ 

**Power** 
$$power = \frac{work}{time} \Rightarrow P = \frac{W}{t}$$

Figure Efficiency 
$$= \frac{t}{total}$$

$$\% \ Efficiency = \frac{output}{input} \times 100$$

$$\triangleright$$
 Weight  $w = mg$ 

5.1. A force of 20 N acting at an angle of  $60^{\circ}$  to the horizontal is used to pull a box through a distance of  $3\ m$ across a floor. How much work is done? **Given Data** 

$$Force = F = 20 N$$
  
 $Angle = \theta = 60^{\circ}$   
 $Distance\ covered = S = 3\ m$ 

To Find

$$Work\ done = W = ?$$

Solution

By using formula of work done

$$W = FS \cos \theta$$
  
 $W = (20)(3) \cos 60^{\circ}$   
 $W = (20)(3)(0.5)$   
 $W = 30 I$ 

5.2. A body moves a distance of 5 metres in a straight line under the action of a force of 8 newtons. If the work done is 20 Joules, find the angle which the force makes with the direction of motion of the body. **Given Data** 

Distance covered = 
$$S = 5 m$$
  
 $Force = F = 8 N$   
 $Work done = W = 20 J$ 

To Find

$$Angle = \theta =$$

Solution

By using formula of work done

$$W = FS \cos \theta$$

$$\cos \theta = \frac{W}{FS}$$

$$\cos \theta = \frac{20}{(8)(5)}$$

$$\cos \theta = \frac{20}{40}$$

$$\cos \theta = 0.5$$

$$\theta = \cos^{-1}(0.5)$$

$$\theta = 60^{\circ}$$

5.3. An engine raises 100 kg of water through a height of 80 m in 25 s. What is the power of the engine? **Given Data** 

Mass of water = 
$$m = 100 kg$$
  
Height raised =  $h = 80 m$   
Time taken =  $t = 25 s$ 

To Find

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By using formula of potential energy

$$E_p = mgh$$
  
 $E_p = (0.16)(10)(20)$   
 $E_p = 32 J$ 

5.6. A  $0.14\ kg$  ball is thrown vertically upward with an initial velocity of  $35\ ms^{-1}$ . Find the maximum height reached by the ball.

Given Data

Mass of ball = 
$$m = 0.14 kg$$
  
Initial velocity =  $v = 35 ms^{-1}$ 

Gravitational acceleration =  $g = 10 \text{ ms}^{-2}$ 

### To Find

 $Maximum\ height\ reached=h=?$ 

## Solution

At the *maximum height*, all the *kinetic energy* of the ball is converted into *potential energy*.

$$E_p = E_k$$

$$mgh = \frac{1}{2}mv^2$$

$$h = \frac{mv^2}{2mg}$$

$$h = \frac{v^2}{2g}$$

$$h = \frac{(35)^2}{2(10)}$$

$$h = \frac{1225}{20}$$

$$h = 61.25$$

5.7. A girl is swinging on a swing. At the lowest point of her swing, she is  $1.2\,m$  from the ground, and at the highest point she is  $2.0\,m$  from the ground. What is her maximum velocity and where?

**Given Data** 

Height at lowest point 
$$=h_1=1.2~m$$
  
Height at highest point  $=h_2=2.0~m$   
Change in height  $=h=h_2-h_1$   
 $h=2.0-1.2$   
 $h=0.8~m$ 

Gravitational acceleration =  $g = 10 \text{ ms}^{-2}$ 

To Find

Maximum velocity = v = ?Location of maximum velocity = ?

## Solution

At the lowest point, all the *potential energy* is converted into *kinetic energy*. So,

$$E_p = E_k$$

$$mgh = \frac{1}{2}mv^2$$

$$\frac{2mgh}{m} = v^2$$

$$2gh = v^2$$

$$v^2 = 2gh$$

$$\sqrt{v^2} = \sqrt{2gh}$$

$$v = \sqrt{(2)(10)(0.8)}$$

$$v = \sqrt{16}$$

$$v = 4 ms^{-1}$$

The maximum velocity is  $4 ms^{-1}$ , and it occurs at the lowest point of the swing.

5.8. A person pushes a lawn mower with a force of 50~N making an angle of  $45^{\circ}$  with the horizontal. If the mower is moved through a distance of 20~m, how much work is done?

**Given Data** 

$$Force = F = 50 N$$
  
 $Angle = \theta = 45^{\circ}$   
 $Distance = S = 20 m$ 

To Find

$$Work\ done = W = ?$$

#### Solution

By using formula of work done

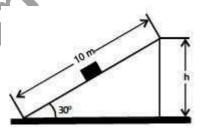
$$W = FS \cos \theta$$

$$W = (50)(20) \cos 45^{\circ}$$

$$W = (50)(20)(0.707)$$

$$W = 707 J$$

- 5.9. Calculate the work done in
- (i) Pushing a 5 kg box up a frictionless inclined plane 10 m long that makes an angle of 30° with the horizontal.



(ii) Lifting the box vertically up from the ground to the top of the inclined plane.

**G**iven Data

$$Mass\ of\ box = m = 5\ kg$$
 
$$Length\ of\ inclined\ plane = S = 10\ m$$
 
$$Angle\ with\ horizontal = \theta = 30^{\circ}$$
 
$$Gravitational\ acceleration = g = 10\ ms^{-2}$$

To Find

Work done along the incline = W = ?Work done in lifting the box vertically = W = ?

Solution (i

The force needed to push the box up the slope is the component of weight along the incline:

$$F = mg \sin \theta$$

Using the formula for work

$$W = FS$$

$$W = (mg \sin \theta)(S)$$

$$W = (5)(10)(\sin 30^{\circ})(10)$$

$$W = (5)(10)(0.5)(10)$$

$$W = 250 I$$

(ii) Given figure forms a right-angle triangle so for height use trigonometric ratio

$$\sin \theta = \frac{Perpendicular}{Hypotenuse}$$

$$\sin 30^{\circ} = \frac{h}{10}$$

$$(10)(\sin 30^{\circ}) = h$$

$$(10)(0.5) = h$$

$$5 = h$$

$$h = 5 m$$

The work done against gravity is equal to the change in potential energy:

$$W = E_p$$
  
 $W = mgh$   
 $W = (5)(10)(5)$   
 $W = 250 J$ 

5.10. A box of mass  $10 \ kg$  is pushed up along a ramp 15 m long with a force of 80 N. If the box rises up a height of 5 m, what is the efficiency of the system? **Given Data** 

Mass of box = 
$$m = 10 kg$$
  
Length of ramp =  $S = 15 m$   
Force applied =  $F = 80 N$   
Height raised =  $h = 5 m$ 

Gravitational acceleration =  $g = 10 \text{ ms}^{-2}$ 

## To Find

Efficiency of the system = ?

### Solution

The total energy supplied is the work done (input). By using formula of work done

$$W_{input} = FS$$
  
 $W_{input} = (80)(15)$   
 $W_{input} = 1200 J$ 

The useful energy is the work done (output) to lift the box to height h.

$$W_{output} = mgh$$
  
 $W_{output} = (10)(10)(5)$   
 $W_{output} = 500 J$ 

By using formula of efficiency

% Efficiency = 
$$\frac{W_{output}}{W_{input}} \times 10^{\circ}$$
  
% Efficiency =  $\frac{500}{1200} \times 100$   
% Efficiency =  $\frac{50000}{1200}$   
% Efficiency = 41.7 %

5.11. A force of 600 N acts on a box to push it 5 m in 15 s. Calculate the power.

**Given Data** 

$$Force = F = 600 N$$
  
 $Distance = S = 5 m$   
 $Time = t = 15 s$ 

$$Power = P = ?$$

# Solution

By using formula of power

Power = 
$$\frac{Work}{time}$$

$$P = \frac{W}{t}$$

$$P = \frac{FS}{t}$$

$$P = \frac{(600)(5)}{15}$$

$$P = 200 \text{ watt}$$

5.12. A 40 kg boy runs up-stair 10 m high in 8 s. What power he developed.

**Given Data** 

Mass of boy = 
$$m = 40 \text{ kg}$$
  
Height =  $h = 10 \text{ m}$   
Time =  $t = 8 \text{ s}$ 

To Find

$$Power = P = ?$$

# Solution

By using formula of power

$$Power = \frac{Work}{time}$$

$$P = \frac{W}{t}$$

$$P = \frac{FS}{t}$$

$$P = \frac{mgh}{t} \quad \because F = W = mg \& S = h$$

$$P = \frac{(40)(10)(10)}{5}$$

$$P = 500 W$$

5.13. A force F acts through a distance L on a body. The force is then increased to 2F that further acts through 2L. Sketch a force-displacement graph and calculate the total work done.

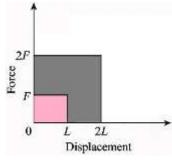
Given Data

Force for distance L = FForce for distance 2L = 2FTo Find

 $Work\ done = W = ?$ 

Solution

As, the area under a forcedistance graph represents the work done by the force



 $Work\ done = Area\ under\ the\ graph$  $= (F \times L) + (2F \times 2L)$ = FL + 4FL= 5FL $Work\ done = 5\ unit$ 

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